

trated between center conductor and lower ground plane, i.e., in the dielectric board, and the velocity goes down.

Finally, the thickness of the dielectric board was changed, again for the three preceding lines. The positions of the center conductor and of the upper edge of the board were kept constant, and the thickness was varied by changing the location of the lower edge of the board. The results for d values of $d=18$, 24, and 30 mils are shown in Fig. 6. The impedance and phase velocity decrease as expected with increasing thickness.

The impedance slope of these curves indicates a Z versus d dependence of

0.39 Ω /mil for the line width $w=72$ mils,
0.32 Ω /mil for the line width $w=120$ mils,
and
0.19 Ω /mil for the line width $w=192$ mils.

As the impedance ratios of the three lines are 1:0.76:0.56 and the Z versus d dependences are 1:0.82:0.49, it follows that a change in d is about equally critical for lower and higher ohmic lines within the range of consideration.

The fractional velocity variation is the same as the fractional impedance variation.

The accuracy of these calculations for Z is typically around 1 percent but not worse than 2 percent, for v/v_0 typically around 0.5 percent but not worse than 1 percent.

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Realizations of a Duo-Pole Branch of an Elliptic-Function Bandstop Filter

This correspondence illustrates six realizations of the TEM line (transformed) equivalent of the LC network A of Fig. 1. Network A is here taken to represent a shunt branch of a low-pass elliptic-function ladder filter [1]. Richards' transformation [2] converts a lumped element low-pass filter to a transmission-line bandstop filter [3]–[6]. Each filter element, L or C, is then replaced by a short- or open-circuited quarter-wave stub. Thus, network A is transformed to network B, with parameters as defined in Fig. 1. The six stripline and reentrant slabline networks C–H are equivalent to network B and are well suited for microwave filters. The characteristic impedances of the lines in networks C, D, E, and H are given in Fig. 1, and the coupled-line impedances of networks F and G are given in Schiffman and Matthaei [5] and Schiffman [7]. Although networks F and G are shown as cascaded sections [5], [7] (not duo-pole type), here they are shunt-connected with the far terminals open circuited. In networks B–D, line Z_1 is short circuited and line

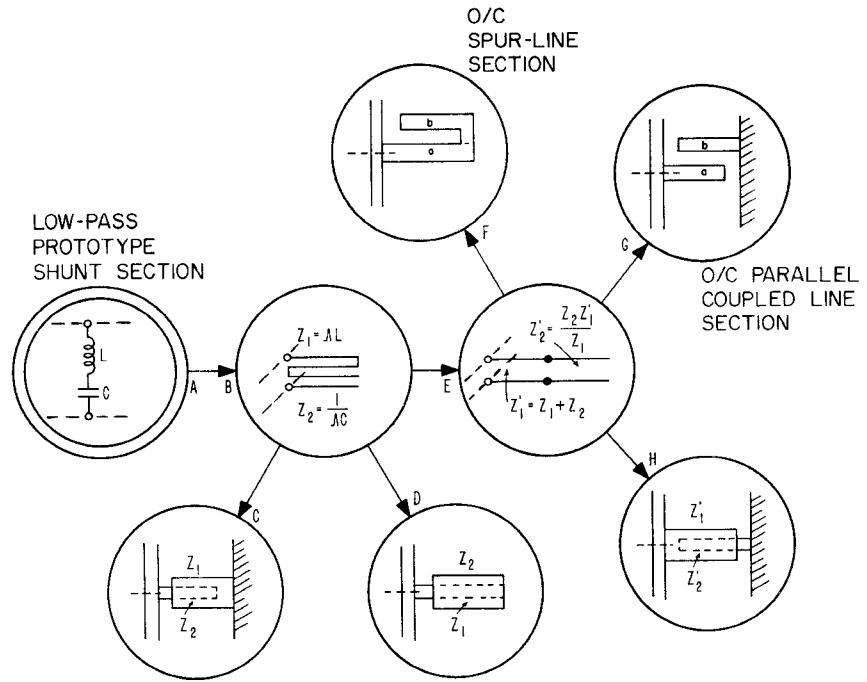


Fig. 1. Stripline and reentrant slabline realizations of a shunt duo-pole branch of an elliptic-function bandstop filter. Here, $\Delta = \omega_1' \tan[(\pi/2)(\omega_0 - \omega_1)/\omega_0]$ where ω_1 and ω_1' are corresponding frequencies (usually taken as band-edge frequencies) in the bandstop and low-pass frequency domains, and ω_0 is center of stopband.

Z_2 is open circuited at its far end, and lines Z_1 and Z_2 are in series with each other at their near ends. In networks E and H, Z_2' is open circuited and in cascade with Z_1' .

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unusual cross section. Specifically, the cross section consisted of a round outer conductor with a center conductor composed of a number of thin fins symmetrically positioned about the axis of the line. Examples of this general class of cross section are illustrated in Fig. 1 for the cases of two, three, four, and six fins. Solutions for the characteristic impedances of this type of configuration were obtained by an interesting series of conformal transformations that mapped the multifin line geometry into that of a symmetric strip transmission line. Since the characteristic impedance of the latter is well known, curves can readily be generated for the multifin line impedance.

The basic steps in the mapping process are outlined in Fig. 2. First, geometries having other than two fins are mapped into the two-fin case by applying the transformation

$$z' = z^{n/2} \quad (1)$$

where n is the number of fins in the given geometry (z plane). Since this transformation maps $2/n$ of the multifin line space into the entire space of the two-fin line, the effect will be to establish the relations

$$Z_n = \frac{2}{n} Z_2 \quad (2)$$

when

$$\frac{r_n}{R_n} = \left(\frac{r_2}{R_2}\right)^{2/n} \quad (3)$$

Characteristic Impedance of Multifin Transmission Lines

Several years ago, the author had occasion to investigate the characteristic impedance properties of a TEM transmission line of

where Z_n , r_n , R_n and Z_2 , r_2 , R_2 are the characteristic impedance, fin radial dimension, and shield radius of the n -fin and two-fin lines, respectively. Note that the z and z' planes are normalized so that the shield lies on the unit circle.